Tripoli university

Faculty of engineering

EE department

EE313 tutorial

Problem#1

Find the flux of the vector field $\vec{A} = \frac{\vec{a}_{\rho}}{\rho}$ for:

- i) The sphere r=a centered at the origin.
- ii) The cube 2a on a side centered at the origin with sides parallel to the coordinate axes.
- iii) The cylinder $0 \le \rho \le 3a$, $0 \le \phi \le 2\pi$, $-a \le z \le a$.

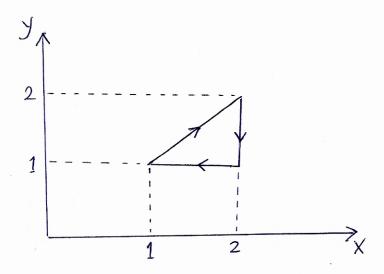
Problem#2

For the parallel plates shown in the fig at time t=0 an electron is emitted from the lower plate with zero initial velocity and upper plate is at 15V higher than the lower. At time t_1 the electron is midway between the plates and the upper plate voltage changes abruptly to -30V. Determine which plate the electron will strike.



Assume the vector function $\vec{A}=\vec{a}_x 3x^2y^3-\vec{a}_y x^3y^2$.

- i) Verify Stoke's theorem for the surface shown in the fig.
- ii) Can \vec{A} be expressed as the gradient of a scalar? Explain.



Problem#4

A flat slab of sulfur $(\epsilon_r=4)$ is placed normal to a uniform field. If the polarization surface charge density ρ_{sp} on the slab surface is 0.5C/m². Find:

- i) Polarization of the slab.
- ii) Flux density in the slab.
- iii) Flux density outside the slab (in air) .
- iv) Field intensity inside and outside the slab.

Problem#5

The plane x+2y-5z=10 separates the region which has $\mu_r=2$ and on it $\vec{H}=5\vec{a}_x+6\vec{a}_y+10\vec{a}_z$ from air. Find \vec{H} in air.

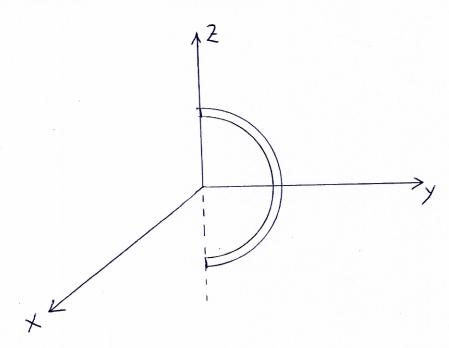
A plane wave at 100MHz is propagating in a lossy material. The phase of the electric field shifts 90^{0} over a distance of 0.5m, and its peak value is reduced by 25% for each meter travelled. Find α , β , v_{p} .

Problem#7

At a certain frequency in copper ($\sigma = 58 \times 10^6 \ S/m$) the phase constant is 3.71X10⁵ rad/m. Determine the frequency.

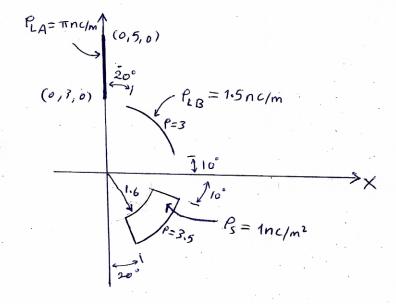
Problem#8

A semi-circular ring lying in the xy plane has a charge density $\rho_l=\rho_0cos\theta$ C/m, where θ is the angle measured from the z-axis as shown in the fig. Find \vec{E} for points (x,0,0) along the x-axis.



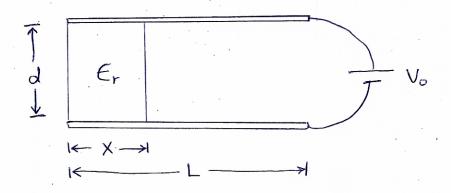
Problem#9

The fig below shows three separate charge distributions in the z=0 plane in free space. Find the potential at P(0,0,6).



A parallel plate capacitor of width w, length L and separation d is partially filled with a dielectric medium of ϵ_r as shown in the fig. A battery of V_0 volts is connected between the plates.

- i) Find \vec{D} , \vec{E} and ρ_S in each region.
- ii) Find distance x such that the electrostatic energy stored in each region is the same.



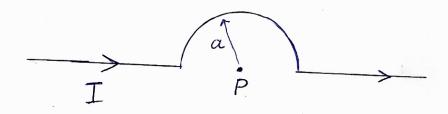
And Lenter 1



Let a filamentary current of 5mA be directed from infinity to the origin on the positive z-axis and then back out to infinity on the positive x-axis. Find \vec{B} at P(0,1,0).

Problem#13

For the current shown. Find the magnetic field at the point P.



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$$\begin{array}{ll}
(28) & \overrightarrow{r} = \overrightarrow{a_y} R \sin \theta + \overrightarrow{a_z} R \cos \theta \\
\overrightarrow{R} = (1) \times \overrightarrow{a_x} - \overrightarrow{a_y} R \sin \theta - \overrightarrow{a_z} R \cos \theta \\
E = \int \frac{f_2 dl}{4\pi |R|^2} \overrightarrow{a_R} = \int \frac{f_2 (G \sin R + G \sin R \cos R)}{4\pi |R|^2} (1) \frac{1}{4\pi |R|^2} \frac{1}{4\pi |R|^2} \left((1) \times \frac{1}{4\pi |R|^2} (1)$$

$$=\frac{-P_0R^2}{8\pi\epsilon(x^2+R^2)^{3/2}}\overrightarrow{a_2}$$

(Q9) ① due to
$$f_{LA}$$

$$\Phi = \int_{4\pi\epsilon_{o}}^{5} \frac{\pi \times 10^{9} \text{ dy}}{4\pi\epsilon_{o} \sqrt{y'_{2}^{2}+6^{2}}} = \frac{10^{3}}{4\times8.854} \ln(y' + \sqrt{y'_{2}^{2}+6^{2}})|_{3}^{5} = 7.83 \text{ V}.$$

(2) due to
$$\ell_{LB}$$

 $\phi = \int \frac{1.5 \times 10^{-9} (3 d\phi)}{4 \pi \epsilon_0 \sqrt{3^2 + 6^2}} = 6.03 \left(\frac{7\pi}{18} - \frac{\pi}{18} \right) = 6.31 \text{ V}$

3 due to
$$l_s$$

$$\phi = \int_{18}^{\frac{7\pi}{18}} \int_{1.6}^{3.5} \frac{10^9 \, \text{p'dp'dd'}}{4\pi\epsilon_0 \sqrt{p'^2 + 6^2}} = \frac{10^9}{4\pi\epsilon_0} \left(\frac{\pi}{3}\right) \int_{1.6}^{\infty} \frac{p' \, dp'}{\sqrt{(p')^2 + 36}} = \frac{10^9}{4\pi\epsilon_0} \left(\frac{\pi}{3}\right) \sqrt{(p')^2 + 36} = 6.93 \, \text{V}$$

$$Q(0) \Rightarrow \overrightarrow{E} = -\overrightarrow{ay} \frac{Vo}{d}$$
 in all space.

 $\overrightarrow{D}(air) = -\overrightarrow{ay} \frac{\epsilon_0 V_0}{d}$, $\overrightarrow{D}(dielectric) = -\overrightarrow{ay} \frac{\epsilon_r \epsilon_0 V_0}{d}$

on top plate: $P_s(air) = \frac{\epsilon_0 V_0}{d}$, $P_s(air) = \frac{\epsilon_r \epsilon_0 V_0}{d}$

$$U = \frac{1}{2} | \mathcal{E} | \mathcal{E} | dV$$

$$U_{\text{dielectric}} = \frac{1}{2} A \mathcal{E}_{r} \mathcal{E}_{s} \int \frac{V_{o}^{2}}{d^{2}} dx = \frac{A \mathcal{E}_{r} \mathcal{E}_{o} V_{o}^{2}}{2 d^{2}} \times$$

$$U_{\text{air}} = \frac{1}{2} A \mathcal{E}_{o} \int \frac{V_{o}^{2}}{d^{2}} dx = \frac{A \mathcal{E}_{o} V_{o}^{2} (L - x)}{2 d^{2}} \times$$

$$V_{\text{air}} = \frac{1}{2} A \mathcal{E}_{o} \int \frac{V_{o}^{2}}{d^{2}} dx = \frac{A \mathcal{E}_{o} V_{o}^{2} (L - x)}{2 d^{2}} \times$$

$$V = \frac{L}{\mathcal{E}_{r} + 1}$$

$$\frac{a}{A} = \frac{\overrightarrow{a_0}}{P} = \frac{\overrightarrow{a_x} \cos \phi + \overrightarrow{a_y} \sin \phi}{\sqrt{x^2 + y^2}} = \frac{x}{x^2 + y^2} \overrightarrow{a_x} + \frac{y}{x^2 + y^2} \overrightarrow{a_y} \qquad \text{rectangular.}$$

$$\frac{A}{A} = \frac{r \sin \theta \cos \phi}{r^2 \sin \theta \cos \phi + r \sin \theta \sin \phi} \left(\overrightarrow{a_r} \sin \theta \cos \phi + a_\theta \cos \theta \cos \phi - a_\phi \sin \phi \right)$$

$$= \frac{\cos\phi}{r\sin\theta} \left(\vec{a_r} \sin\theta \cos\phi + \vec{a_\theta} \cos\theta \cos\phi \right) + \frac{\sin\phi}{r\sin\theta} \left(\vec{a_r} \sin\theta \sin\phi + \vec{a_\theta} \cos\theta \sin\phi \right)$$

 $\int \frac{dx}{x^2 + a^2} = \frac{1}{\alpha} t cm^2 \left(\frac{x}{\alpha}\right)$

$$= \overrightarrow{a_r} \left(\frac{\cos^2 \phi}{r} + \frac{\sin \phi}{r} \right) + \overrightarrow{a_\theta} \left(\cos \phi + \frac{\cos \theta}{r \sin \theta} + \sin^2 \phi + \frac{\cos \theta}{r \sin \theta} \right)$$

$$\oint A \cdot ds = \iint a \sin\theta d\theta d\phi = 4\pi q$$

$$\oint a \sin\theta d\theta d\phi = 4\pi q$$

$$\oint A \cdot ds = \iint \frac{a}{x^2 + a^2} dy dx$$

$$+\int_{a}^{a} \frac{a}{y+a^{2}} \frac{a}{-a} \frac{dxy+\int_{a}^{a} \frac{a}{x^{2}+a^{2}} \frac{dx}{x^{2}+a^{2}} \frac{dx}{x^{2}+a^{2}}$$

=
$$8a \tan^{3}(\frac{x}{a}) \Big|_{-9}^{9} = 9a(\tan^{3}(1) - \tan^{3}(-1)) = 8a(\frac{\pi}{2}) = 4\pi a.$$

